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## PSPLIB – A project scheduling problem library <sup>1</sup>

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### Abstract

We present a set of benchmark instances for the evaluation of solution procedures for single- and multi-mode resource-constrained project scheduling problems. The instances have been systematically generated by the standard project generator ProGen. They are characterized by the input-parameters of ProGen. The entire benchmark set including its detailed characterization and the best solutions known so far are available on a public ftp-site. Hence, researchers can download the benchmark sets they need for the evaluation of their algorithms. Additionally, they can make available new results. Depending on the progress made in the field, the instance library will be continuously enlarged and new results will be made accessible. This should be a valuable and driving source for further improvements in the area of project type scheduling.

*Keywords:* Project scheduling; Resource constraints; Benchmark instances

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### 1. Introduction

Whereas the standard methods of project scheduling, CPM and MPM, base on the assumption of unlimited capacity of resources, modern approaches include the more realistic limitation of the resources' availabilities.

Consequently, numerous publications have dealt with exact and heuristic methods for solving the so-called single-mode resource-constrained project scheduling problem (SMRCPSP) where each of the activities of the project has to be performed in one prescribed way (mode) using specified amounts of the resources provided. The most common objective of the SMRCPSP is the minimization of the makespan (cf. e.g., [3,4,5,24,32]).

Recent developments have incorporated more reality by allowing the activities to be executed in one

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<sup>1</sup> The project generator ProGen, a detailed description of ProGen [17], the instance-sets, their characterizations as well as the optimal or presently best known objective function values are available on the ftp-site [ftp.bwl.uni-kiel.de](ftp://ftp.bwl.uni-kiel.de/pub/operations-research/psplib) under the path `/pub/operations-research/psplib`; access via the WWW is available under <ftp://ftp.bwl.uni-kiel.de/pub/operations-research/psplib/>. New results, comments, and questions can be communicated to the email address [psplib@bwl.uni-kiel.de](mailto:psplib@bwl.uni-kiel.de).

Public domain software in OR can be contributed to ORSEP by sending a diskette containing the code and the code description to Professor H.W. Hamacher, Department of Mathematics, University of Kaiserslautern, P.O. Box 3049, D-67653 Kaiserslautern, Germany, email: [hamacher@mathematik.uni-kl.de](mailto:hamacher@mathematik.uni-kl.de).

Copies of published codes can be requested from the same address or directly from the authors by sending a formatted diskette and a self-addressed envelope. See EJOR 48(1) (1990) 161–162, for details.

out of several modes. The modes reflect alternative combinations of resources and belonging quantities employed to fulfill the tasks related to the activities. The activity duration is a discrete function of the employed quantities, that is, using this concept, e.g., an activity can be accelerated by raising the quantities coming into operation (time-resource-tradeoff). Moreover, by raising the required quantities of some resources while reducing the required quantities of others, the resource substitution (resource-resource-tradeoff) can be realized. The problem at hand is the multi-mode resource-constrained project scheduling problem (MMRCPS) which is commonly considered with makespan minimization as objective too (cf. [22,23,28,29,31,34]).

Using the categorization scheme proposed by Slowinski (cf. [26,27]) and Weglarz (cf. [35,36]) three categories of resources required for the execution of a project are distinguished, namely: renewable, nonrenewable, and doubly constrained resources.

Renewable resources are available on a period-by-period basis, that is, the quantities available are renewed from period to period (hour, day, week, month). The per-period availability is assumed constant. E.g., manpower, machines, fuelflow and space are renewable resources.

In contrast to the renewable resources, nonrenewable ones are limited on a total project basis, that is, instead of the limited per-period usage of the renewable resources we have a limited overall consumption of the nonrenewable resources for the entire project. Money, energy and raw material belong to this category.

Resources which are limited on total project basis as well as on per-period basis are called doubly constrained. Money represents a resource of this category if beside the project's budget the per-period cashflow is limited. Manpower can be a doubly constrained resource, too, if for example a skilled worker can spend only a limited number of periods on the project. Clearly, since the doubly constrained resources can easily be taken into account by appropriately enlarging the sets of renewable and nonrenewable resources, respectively, they do not have to be considered explicitly.

The remaining of the paper is organized as follows: Section 2 describes the resource-constrained

project scheduling problem in detail and presents an integer programming formulation. Section 3 introduces the parameters used for characterizing the instances generated. Section 4 provides the characterization of the benchmark sets and the nomenclature. Section 5 summarizes research performed on the instance sets. Finally, Section 6 specifies how new benchmark results can be made available to the research community.

## 2. The model

We consider a project which consists of  $J$  activities (jobs, tasks). Due to technological requirements precedence relations between some of the activities enforce that an activity  $j$ ,  $j = 2, \dots, J$ , may not be started before all its predecessors  $h$ ,  $h \in \mathcal{P}_j$ , are finished. The structure of the project is depicted by a so-called activity-on-node (AON) network where the nodes represent the activities and the arcs the precedence relations. The network is acyclic and numerically labelled, that is, an activity has always a higher label than all its predecessors. W.o.l.o.g. activity 1 is the only start activity (source) and activity  $J$  is the only finish activity (sink). Both have a single mode with zero duration and resource request; they are dummy activities.

The activities  $j$ ,  $j = 1, \dots, J$ , have to be executed in one out of  $M_j$  modes. The activities may not be preempted and a mode once selected may not change, i.e., an activity  $j$  once started in mode  $m$  has to be completed in mode  $m$  without interruption. Performing activity  $j$  in mode  $m$  takes  $d_{jm}$  periods and is supported by a set  $R$  and  $N$  of renewable and nonrenewable resources, respectively. Considering a horizon, that is, an upper bound  $\bar{T}$  on the project's makespan,  $K_r^p$  units of renewable resource  $r$ ,  $r \in R$ , are available in period  $t$ ,  $t = 1, \dots, \bar{T}$ . The overall capacity of the nonrenewable resource  $r$ ,  $r \in N$ , is given by  $K_r^v$ . If activity  $j$  is scheduled in mode  $m$ , then  $k_{jmr}^p$  units of the renewable resource  $r$ ,  $r \in R$ , are used each period activity  $j$  is in process. Additionally,  $k_{jmr}^v$  units of the nonrenewable resource  $r$ ,  $r \in N$ , are consumed. The parameters are summarized in Table 1 and assumed to be integer-valued.

The objective is to find a makespan minimal schedule that meets the constraints imposed by the

Table 1  
Symbols and definitions

$J$	: Number of activities.
$M_j$	: Number of modes activity $j$ can be performed in.
$d_{jm}$	: Duration of activity $j$ being performed in mode $m$ .
$R(N)$	: Set of renewable (nonrenewable) resources.
$\bar{T}$	: Upper bound on the project's makespan.
$K_r^p \geq 0$	: Number of units of renewable resource $r$ , $r \in R$ , available in period $t$ , $t = 1, \dots, \bar{T}$ .
$K_r^v \geq 0$	: Total number of units available of nonrenewable resource $r$ , $r \in N$ .
$k_{jmr}^p \geq 0$	: Number of units of renewable resource $r$ , $r \in R$ , used by activity $j$ being performed in mode $m$ each period the activity is in process.
$k_{jmr}^v \geq 0$	: Number of units of nonrenewable resource $r$ , $r \in N$ , consumed by activity $j$ being performed in mode $m$ .
$\mathcal{P}_j (\mathcal{S}_j)$	: Set of immediate predecessors (successors) of activity $j$ .
$ES_j (EF_j)$	: Earliest start time (finish time) of activity $j$ , calculated by using minimal activity durations and neglecting resource usage (consumption).
$LS_j (LF_j)$	: Latest start time (finish time) of activity $j$ , calculated by using minimal activity durations, neglecting resource usage (consumption) and taking into account the upper bound $\bar{T}$ on the project's duration.

precedence relations and the limited resource availabilities.

Due to the constant per-period availability of the renewable resources, an upper bound  $\bar{T}$  on the project's minimum makespan can be determined by the sum of the maximum activity durations. Given  $\bar{T}$  we can use the precedence relations and the modes of

shortest duration to calculate time windows, i.e., intervals  $[EF_j, LF_j]$ , with earliest finish times  $EF_j$  and latest finish times  $LF_j$ , containing the precedence feasible completion times of activity  $j$ ,  $j = 1, \dots, J$ , by traditional forward and backward recursion as performed by MPM.

With the time windows derived we can state the

Table 2  
The model of the MMRCPS

Minimize	$\Phi(x) = \sum_{m=1}^{M_j} \sum_{t=EF_j}^{LF_j} t \cdot x_{jmt}$	(1)
s.t.		
	$\sum_{m=1}^{M_j} \sum_{t=EF_j}^{LF_j} x_{jmt} = 1, \quad j = 1, \dots, J,$	(2)
	$\sum_{m=1}^{M_h} \sum_{t=EF_h}^{LF_h} t \cdot x_{hmt} \leq \sum_{m=1}^{M_j} \sum_{t=EF_j}^{LF_j} (t - d_{jm}) x_{jmt}, \quad j = 2, \dots, J, \quad h \in \mathcal{P}_j,$	(3)
	$\sum_{j=1}^J \sum_{m=1}^{M_j} k_{jmr}^p \sum_{q=\max\{t, EF_j\}}^{\min\{t+d_{jm}-1, LF_j\}} x_{jmq} \leq K_r^p, \quad r \in R, \quad t = 1, \dots, \bar{T},$	(4)
	$\sum_{j=1}^J \sum_{m=1}^{M_j} k_{jmr}^v \sum_{t=EF_j}^{LF_j} x_{jmt} \leq K_r^v, \quad r \in N,$	(5)
	$x_{jmt} \in \{0, 1\}, \quad j = 1, \dots, J, \quad m = 1, \dots, M_j, \quad t = EF_j, \dots, LF_j.$	(6)

problem as a linear program as similarly presented by Talbot (cf. [34]). We use binary decision variables  $x_{jmt}$ ,  $j = 1, \dots, J$ ;  $m = 1, \dots, M_j$ ;  $t = EF_j, \dots, LF_j$ ,

$$x_{jmt} = \begin{cases} 1 & \text{if activity } j \text{ is performed in mode } m \\ & \text{and completed at the end of period } t, \\ 0, & \text{otherwise.} \end{cases}$$

The model is presented in Table 2 and is referred to as the multi-mode resource-constrained project scheduling problem (MMRCPSp).

Since there is exactly one finish activity, the objective function (1) realizes the minimization of the project's makespan. Constraints (2) ensure that exactly one mode and one completion time is assigned to each activity. The precedence relations are taken into account by (3). (4) guarantees that the per-period availabilities of the renewable resources are not exceeded. Finally, (5) secures feasibility with respect to the consumable (nonrenewable) resources.

Obviously, given  $M_j = 1$ ,  $j = 1, \dots, J$ , and  $|N| = 0$ , the MMRCPSp degenerates to the single-mode resource-constrained project scheduling problem (SMRCPSp). Moreover, the well-known flow-shop, job-shop, and open-shop problems are included in the model outlined. Thus, the problem is a member of the class of NP-hard problems (cf. [12]). Furthermore, if  $|N| > 1$ , then the feasibility problem (2)–(6) is NP-complete (cf. [15]).

### 3. Project characteristics

In this section we give a brief summary of the characteristics of the project instances, that is, the parameters of ProGen. A detailed description of the parameters and their realization can be found in [17] and [18].

$J^{\min}$  ( $J^{\max}$ ) = Minimum (maximum) number of non-dummy activities the project comprises.

$M_j^{\min}$  ( $M_j^{\max}$ ) = Minimum (maximum) number of modes an activity  $j$ ,  $j = 2, \dots, J - 1$ , can be performed in.

$d^{\min}$  ( $d^{\max}$ ) = Minimum (maximum) duration of an activity  $j$ ,  $j = 2, \dots, J - 1$ .

$R^{\min}$  ( $R^{\max}$ ) = Minimum (maximum) number of renewable resources to be taken into account.

$N^{\min}$  ( $N^{\max}$ ) = Minimum (maximum) number of nonrenewable resources to be taken into account.

$\mathcal{S}_1^{\min}$  ( $\mathcal{S}_1^{\max}$ ) = Minimum (maximum) number of start activities.

$\mathcal{F}_j^{\min}$  ( $\mathcal{F}_j^{\max}$ ) = Minimum (maximum) number of finish activities.

$\mathcal{S}_j^{\max}$  ( $\mathcal{P}_j^{\max}$ ) = Maximum number of successors (predecessors) of an activity  $j$ ,  $j = 2, \dots, J - 1$ .

NC = Network complexity, i.e., the average number of non-redundant arcs per node including the dummy activities. The number of arcs actually incorporated into the network ActArcs is controlled by  $\epsilon_{\text{NET}}$ , the network complexity deviation tolerance, such that

$$\text{ActArcs} \in [J \cdot \text{NC} \cdot (1 - \epsilon_{\text{NET}}); J \cdot \text{NC} \cdot (1 + \epsilon_{\text{NET}})].$$

$Q_\tau^{\min}$  ( $Q_\tau^{\max}$ ) = minimum (maximum) number of resources of category  $\tau$ ,  $\tau \in \{R, N\}$ , used and consumed, respectively, by an activity-mode combination  $[j, m]$ ,  $j = 2, \dots, J - 1$ ;  $m = 1, \dots, M_j$ , i.e., minimum and maximum power of the sets  $Q_{jm}^\tau = \{[j, m, r]; k_{jmr} > 0, r \in \tau, j = 2, \dots, J - 1; m = 1, \dots, M_j\}$ .

$U_\tau^{\min}$  ( $U_\tau^{\max}$ ) = minimum (maximum) level of per-period usage and total consumption, respectively, of resource  $r$ ,  $r \in \tau$ ,  $\tau \in \{R, N\}$ , by an activity-mode combination  $[j, m]$  with  $[j, m, r] \in Q_{jm}^\tau$ ,  $j = 2, \dots, J - 1$ ,  $m = 1, \dots, M_j$ .

$P_1^\tau$  ( $P_2^\tau$ ) = probability that the level of per-period usage and total consumption, respectively, of a resource of category  $\tau$ ,  $\tau \in \{R, N\}$ , is duration constant (monotonically decreasing with the duration).

$\text{RF}_\tau$  = Resource factor of resources of category  $\tau$ ,  $\tau \in \{R, N\}$ .  $\text{RF}_\tau$  reflects the average portion of the resources of category  $\tau$ ,  $\tau \in \{R, N\}$ , used and consumed, respectively. More precisely, the actual resource factor  $\text{ARF}_\tau$  of a project instance is given by

$$\text{ARF}_\tau = \frac{1}{J - 2} \sum_{j=2}^{J-1} \frac{1}{M_j} \frac{1}{|\tau|} \sum_{m=1}^{M_j} |Q_{jm}^\tau|.$$

and it is controlled by  $\epsilon_{RF}$ , the resource factor deviation tolerance, such that

$$ARF_r \in [(1 - \epsilon_{RF}) \cdot RF_r; (1 + \epsilon_{RF}) \cdot RF_r].$$

$RS_\tau$  = Resource strength of resources of category  $\tau$ ,  $\tau \in \{R, N\}$ .  $RS_\tau$  measures the strength of the resource constraints of type  $\tau$ . It is a scaling parameter expressing resource availability  $K_r^\tau$  as a convex combination of a minimum and maximum level  $K_r^{\min}$  and  $K_r^{\max}$ ,  $r \in \tau$ , respectively. Using the function  $\text{round}(\cdot)$ , that rounds a real value to an integer, it is given by

$$K_r^\tau = K_r^{\min} + \text{round}(RS_\tau (K_r^{\max} - K_r^{\min})).$$

For a nonrenewable resource  $r$ ,  $r \in N$ , the minimum level  $K_r^{\min}$  and maximum level  $K_r^{\max}$  is obtained by cumulating the consumptions obtained when performing each activity in the mode having minimum and maximum consumptions, respectively, that is,

$$K_r^{\min} = \sum_{j=2}^{J-1} \min_{m=1}^{M_j} \{k_{jmr}^v\},$$

$$K_r^{\max} = \sum_{j=2}^{J-1} \max_{m=1}^{M_j} \{k_{jmr}^v\}.$$

For a renewable resources  $r$ ,  $r \in R$ , the minimum level  $K_r^{\min}$  is the lowest availability level allowing resource feasibility with respect to the considered resource, that is,

$$K_r^{\min} = \max_{j=2}^{J-1} \min_{m=1}^{M_j} \{k_{jmr}^p\}$$

The maximum level  $K_r^{\max}$  is determined via the resource dependant earliest start schedule obtained when performing the activities  $j$ ,  $j = 2, \dots, J - 1$ , in the lowest indexed modes  $m_{jr}^*$  having maximum per-period usage of the considered resource, that is,

$$m_{jr}^* = \min \left\{ m \in \{1, \dots, M_j\}; \right. \\ \left. \times k_{jmr}^p = \max_{m=1}^{M_j} \{k_{jmr}^p\} \right\}$$

$K_r^{\max}$  is determined by the peak per-period usage of resource  $r$  in the resource dependant earliest start schedule.

#### 4. Characterization of the benchmark instances

In this section we present the parameter settings used for generating the benchmark instances. Currently, 2 benchmark sets are available for the SMRCPS and 25 benchmark sets for the MMRCPS. We group the input parameters given in Section 3 into three classes: First, fixed parameters which are constant for all benchmark sets, second, base parameters mainly one of which is adjusted individually for each benchmark set, and third, variable parameters which are systematically varied within each benchmark set. Table 3 gives the fixed parameters.

The instances for the SMRCPS have been generated with the fixed, base, and variable parameter settings given in Tables 3, 4, and 5, respectively. Utilizing a full factorial design of the variable parameters  $NC$ ,  $RF_r$ , and  $RS_r$  with 10 replications per cell we have generated a total of  $3 \cdot 4 \cdot 4 \cdot 10 = 480$  benchmark problems for each set. Table 6 provides a summary of the instances produced.

The 1st column (instance set) gives the prefix of the file names the instances are stored under, the 2nd column ( $P$ ) displays the range of the cell index, reflecting the combination of the variable parameters. The 3rd column ( $E$ ) specifies the range of the instance index within a cell. The 4th column abbreviates the acronym SMRCPS to SM and serves as the suffix of the filenames. The 5th column shows the varied base parameters, here the number of activities which has been set to 30 and 60, respectively. The 6th column refers to the table with the variable parameter levels employed. The 7th column displays the number of instances within the benchmark set. Finally, the 8th column shows how solutions of the benchmark sets have been obtained. A complete file name, e.g., J3012\_10.SM, corresponds to instance set J30, variable parameter combination 12, and problem number 10 of the SMRCPS. The level of the variable parameter settings for each parameter cell index can be found in the file PAR.SM. Optimal

Table 3  
Fixed parameter setting – SMRCPS and MMRCPS

$P_1^R$	$P_2^R$	$P_1^N$	$P_2^N$	$\epsilon_{NET}$	$\epsilon_{RF}$
0.00	1.00	0.00	1.00	0.05	0.05

Table 4  
Base parameter setting – SMRCPSP

	$J$	$M_j$	$d_j$	$R$	$U_R$	$Q_R$	$N$	$U_N$	$Q_N$	$\mathcal{S}_1$	$\mathcal{S}_j$	$\mathcal{P}_j$	$\mathcal{D}_j$
min	30	1	1	4	1	1	0	0	0	3	1	3	1
max	30	1	10	4	10	4	0	0	0	3	3	3	3

objective function values for the instances of the J30 benchmark set have been obtained by [6] and are documented in the file J30OPT.SM. Currently, the instance set J60 cannot be solved by exact solution procedures. Hence, the best objective function values known so far have been computed with the heuristic of [16]. They can be found in the file J60HRS.SM.

Note, originally in [17] the instances J30 [1..48]\_[1..10].SM were named J30[17..64]\_[1..10].

Table 5  
Variable parameter settings – SMRCPSP

Parameter	Levels			
NC	1.50	1.80	2.10	
RF <sub>R</sub>	0.25	0.50	0.75	1.00
RS <sub>R</sub>	0.20	0.50	0.70	1.00

Table 6  
Instance sets – SMRCPSP

Instance set	$P$	$E$	Type	Varied base parameter Table 4	Variable setting	Number of instances	Solution obtained by
J30	[1..48]	[1..10]	SM	$J^{\min} = J^{\max} = 30$	Table 5	480	opt.[6]
J60	[1..48]	[1..10]	SM	$J^{\min} = J^{\max} = 60$	Table 5	480	hrs.[16]

Table 7  
Base parameter setting – MMRCPSP

	$J$	$M_j$	$d_j$	$R$	$U_R$	$Q_R$	$N$	$U_N$	$Q_N$	$\mathcal{S}_1$	$\mathcal{S}_j$	$\mathcal{P}_j$	$\mathcal{D}_j$	NC
min	16	3	1	2	1	1	2	1	1	3	1	3	1	1.8
max	16	3	10	2	10	2	2	10	2	3	3	3	3	1.8

Table 8  
Variable parameter settings – MMRCPSP

	A levels			B levels				C levels					
RF <sub>R</sub>	0.50	1.00		0.50	1.00			0.50	1.00				
RS <sub>R</sub>	0.20	0.50	0.70	1.00	0.25	0.50	0.75	1.00	0.25	0.50	0.75	1.00	
RF <sub>N</sub>	0.50	1.00			0.50	1.00							
RS <sub>N</sub>	0.20	0.50	0.70	1.00	0.25	0.50	0.75	1.00					

DAT and now have been renamed in the library for purposes of standardization.

The instance sets for the MMRCPSP are displayed in Table 9. They have been generated with the fixed, base, and variable parameter settings given in Tables 3, 7, and 8, respectively. Note the slight corruption in denoting the network complexity NC within the base parameter setting of Table 7.

As for the single-mode case, we have generated 10 instances per cell defined by the variable parameter setting. Moreover, we have varied several base parameters as given in the 5th column of Table 9. For technical reasons, beside the base parameter varied, minor adaptations of depending base parameters have been necessary to generate the instance set R1 to R5 and N0 to N3, respectively. More pre-

Table 9  
Instance sets – MMRCPSP

Instance set	$P$	$E$	Type	Varied base parameter Table 7	Variable setting	Number of instances	Solutions obtained by
J10	[1..64]	[1..10]	MM	$J^{\min} = J^{\max} = 10$	Table 8, A	536	opt.[31]
J12	[1..64]	[1..10]	MM	$J^{\min} = J^{\max} = 12$	Table 8, B	547	opt.[31]
J14	[1..64]	[1..10]	MM	$J^{\min} = J^{\max} = 14$	Table 8, B	551	opt.[31]
J16	[1..64]	[1..10]	MM	$J^{\min} = J^{\max} = 16$	Table 8, B	550	opt.[31]
J18	[1..64]	[1..10]	MM	$J^{\min} = J^{\max} = 18$	Table 8, B	552	opt.[31]
J20	[1..64]	[1..10]	MM	$J^{\min} = J^{\max} = 20$	Table 8, B	554	opt.[31]
J30	[1..64]	[1..10]	MM	$J^{\min} = J^{\max} = 30$	Table 8, B	640	hrs.[15, 31]
M1	[1..64]	[1..10]	MM	$M_j^{\min} = M_j^{\max} = 1$	Table 8, B	640	opt.[31]
M2	[1..64]	[1..10]	MM	$M_j^{\min} = M_j^{\max} = 2$	Table 8, B	551	opt.[31]
M4	[1..64]	[1..10]	MM	$M_j^{\min} = M_j^{\max} = 4$	Table 8, B	555	opt.[31]
M5	[1..64]	[1..10]	MM	$M_j^{\min} = M_j^{\max} = 5$	Table 8, B	558	opt.[31]
C15	[1..64]	[1..10]	MM	NC = 1.5	Table 8, B	551	opt.[31]
C21	[1..64]	[1..10]	MM	NC = 2.1	Table 8, B	552	opt.[31]
R1	[1..64]	[1..10]	MM	$R^{\min} = R^{\max} = 1$	Table 8, B	553	opt.[31]
R3	[1..64]	[1..10]	MM	$R^{\min} = R^{\max} = 3$	Table 8, B	557	opt.[31]
R4	[1..64]	[1..10]	MM	$R^{\min} = R^{\max} = 4$	Table 8, B	552	opt.[31]
R5	[1..64]	[1..10]	MM	$R^{\min} = R^{\max} = 5$	Table 8, B	546	opt.[31]
N0	[1..8]	[1..10]	MM	$J^{\min} = J^{\max} = 10$	Table 8, C	75	opt.[31]
N0	[9..16]	[1..10]	MM	$J^{\min} = J^{\max} = 12$	Table 8, C	77	opt.[31]
N0	[17..24]	[1..10]	MM	$J^{\min} = J^{\max} = 14$	Table 8, C	79	opt.[31]
N0	[25..32]	[1..10]	MM	$J^{\min} = J^{\max} = 16$	Table 8, C	79	opt.[31]
N0	[33..40]	[1..10]	MM	$J^{\min} = J^{\max} = 18$	Table 8, C	80	opt.[31]
N0	[41..48]	[1..10]	MM	$J^{\min} = J^{\max} = 20$	Table 8, C	79	opt.[31]
N1	[1..64]	[1..10]	MM	$N^{\min} = N^{\max} = 1$	Table 8, B	637	opt.[31]
N3	[1..64]	[1..10]	MM	$N^{\min} = N^{\max} = 3$	Table 8, B	600	opt.[31]

cisely, if required, we have adapted  $R^{\min}$ ,  $R^{\max}$ ,  $N^{\min}$ ,  $N^{\max}$ ,  $Q_R^{\min}$ ,  $Q_R^{\max}$ ,  $Q_N^{\min}$ ,  $Q_N^{\max}$ ,  $U_N^{\min}$ ,  $U_N^{\max}$ ,  $RF_N$ , and  $RS_N$ . Note, in accordance with the systematic giving of names, the instance set J16 could also be named M3, C18, R2, and N2.

Again, the variable parameter combination related to a cell can be found in the files PAR.MM. All the benchmark sets but J30 have been optimally solved with the branch-and-bound procedure presented in [30,31]. The objective function values are available in the corresponding XYZOPT.MM files, e.g. J10OPT.MM. The instance set J30 has been heuristically solved by the truncated branch-and-bound algorithm of [30,31] with an allotted CPU-time of 60 seconds and by the local search method of [15], respectively. The best objective function values are documented in the file J30HRS.MM.

Note, once more, for standardizational purpose we have renamed the files originally presented in [17] from MM[1..64]\_[1..10].DAT to J10[1..64]\_[1..10].MM.

Contrary to the single-mode case, due to mode-coupling via resource constraints, some of the multi-mode instances do not have a feasible solution (cf. [18]). Infeasible instances detected so far have been removed from the instance sets.

## 5. Use of the instance sets and state-of-the-art results

Since the presentation of the project generator ProGen, the instances produced for its evaluation, i.e. J30[1..48]\_[1..10].SM and J10[1..64]\_

[1..10].MM, as well as additionally generated problem sets have been used in numerous publications. In the following we give a brief summary.

### 5.1. Single mode instances

Kolisch et al. [17,18] solved the instance set J30 with the exact solution procedure of Demeulemeester and Herroelen (cf. [5]) for studying the influence of the variation of project characteristics, like the number of activities  $J$ , the number of renewable resources  $|R|$ , the resource factor  $RF_R$ , the resource strength  $RS_R$ , and the network complexity NC, on the computation time of the exact branch-and-bound procedure. As to be expected, solution times have been positively correlated with the number of jobs and the number of renewable resources. Moreover, a negative correlation of the CPU-time and the resource strength  $RS_R$  as well as a positive correlation of the CPU-time and the resource factor  $RF_R$  have been detected. The negative correlation between the network complexity NC and the CPU-time has not been significant. Numerous of the ProGen instances have not been solved to optimality within 3600 CPU-seconds on a personal computer (80386sx processor, 15MHz clockpulse). On the other hand, the Patterson benchmark set (cf. [21]), though having nearly the same size as the ProGen instances, has been solved to optimality in considerably less average CPU-time on the same computer.

In [19] Mingozzi et al. have used the instance set J30 for testing a recently developed branch-and-bound approach and new bounds. They claim that their algorithm performs better than the one of Demeulemeester and Herroelen (cf. [5]), especially when trying to solve the hard instances which could not be solved by Demeulemeester and Herroelen within the allotted time of 3600 CPU-seconds.

The procedure currently state-of-the-art is the revised and enhanced branch-and-bound procedure of Demeulemeester and Herroelen (cf. [6]). The new version improves its predecessor by the additional implementation of a variant of the Mingozzi et al. bound. Moreover it exploits the 32 bit architecture of an IBM PS/2 Model P75 (80486 processor, 25 MHz clockpulse, 32MB memory) operating under Windows NT. The entire set of instances J30 has

been solved for the first time. Using 24 MB of data memory the computation time is about 33.68 seconds on average.

Kolisch [13] has performed a rigorous experimental investigation of the two basic heuristic scheduling strategies, serial and parallel scheduling, employed in a single-pass as well as in a (biased) random sampling approach. From the instance set J30 he has used those instances, which are resource-constrained, i.e.,  $RS_R < 1$ , and the optimal solutions of which are known from the analysis in [17]. Kolisch has found out that the performance-ranking of priority rules does not differ for single-pass scheduling and sampling, that sampling improves the performance of single-pass scheduling, and that parallel scheduling is not superior in general. In [14] Kolisch has analyzed four new and four well-known priority rules for deterministic parallel scheduling on the subset of the benchmark set J30 described above. The newly developed worst case slack rule has provided the best results. The average deviation from the optimal objective function value has been 4.27% compared to 4.83% of LFT, the best classical rule. An adaptive search method for the RCPSP has been proposed by Kolisch and Drexl (cf. [16]) and again benchmarked on the specified subset. The procedure has achieved an average deviation from optimum of 0.71%.

Naphade et al. (cf. [20]) introduced a local search heuristic for the RCPSP which builds up on ideas of Storer et al. (cf. [33]) for the job shop problem. They have benchmarked the approach on those problems of the instance set J30, which have been optimally solved in [17,18]. The average deviation from the optimal objective function value has been 0.28%.

Some scientists have used the project generator ProGen in order to generate project scheduling instances for their special needs. De Reyck and Herroelen (cf. [7]) utilized ProGen for creating 6000 assembly line balancing problems (ALB). They have assessed the efficiency of resource-constrained project scheduling techniques for solving ALB-type problems. Furthermore, the same authors (cf. [8]) have analyzed the impact of the network structure on solution times. For experimental purposes they have generated 2500 instances. Icmeli and Erenguc (cf. [10]) have generated modified ProGen-instances in order to study the SMRCPSP with discounted cash flows. They have tested their exact branch-and-bound



procedure which employs the branching scheme devised in [5] and derives bounds by solving the resource unconstrained payment scheduling problem with the method given in [9]. Icmeli and Ron (cf. [11]) have created ProGen-instances for problems with relaxed integrality assumptions on the project's time line and activity durations, respectively. Solutions have been derived with the optimization package OSL.

Finally, Schwindt (cf. [25]) extended the project generator ProGen to ProGen/max capable of generating problem instances with minimal and maximal time lags between activities.

### 5.2. Multi-mode instances

The multi-mode benchmark set J10 has been optimally solved by the basic version of the precedence tree guided enumeration scheme (cf. [22,28]) and by the algorithms presented in [29], [30], and [31]. The remaining multi-mode instance sets have been employed for the evaluation of the solution procedure presented in [30] and [31]. The outlined algorithm currently provides the most powerful and general multi-mode approach. It is capable of solving the instance set J20 within an average CPU-time of less than four minutes on a personal computer (80 486 processor, 66 MHz, 16 MB memory). Moreover, the related truncated method shows reasonable heuristic capabilities. It has solved all the instances of the set J10 to optimality and it has determined a feasible solution for 519 of the 640 instances of the set J30 within 60 CPU-seconds. The deviation of the makespan from the precedence-based lower bound averages at 30.84%.

Kolisch and Drexl (cf. [15]) have solved the J10 and J30 multi-mode benchmark sets with a local search heuristic specifically developed to tackle problems with highly constrained nonrenewable resources. The procedure has derived feasible solutions for all problems of the instance set J10 and for 550 problems of J30, respectively. The deviation from optimal solutions of J10 and precedence based lower bounds of J30 averages at 1.75% and 21.01%, respectively.

Additionally, the project generator ProGen has been used for producing instances for variants of the MMRCPSp. In [1] and [2], Ahn and Erenguc have

combined the MMRCPSp and the Time/Cost Trade-off Problem to the so-called multi-mode resource-constrained project scheduling problem with crashable modes, where a given mode duration can be reduced at some cost. The objective is the minimization of the project costs made of the sum of activity and penalty costs. Ahn and Erenguc proposed an exact solution procedure of the branch-and-bound type using some sort of LP-relaxation and an underestimation of the objective function. The procedure has been tested on 160 newly created instances with problem specific adaptations. The authors report that the algorithm outperforms an adapted version of [28].

## 6. Further development of the problem library

The further extension of the problem library depends on the progress made in the development of heuristic and exact solution procedures. We plan to continuously extend the problem library to problems with characteristics similar to the ones already presented, but larger with respect to the number of activities, the number of modes, and the number of resources, respectively. Results obtained on the instances can be communicated to the research community as follows:

Table 10  
Format – Heuristic solutions

Authors' name	:Rainer Kolisch / Arno Sprecher	
Authors' e-mail	:psplib@bwl.uni-kiel.de	
Instance set	:XYZ	
Type	:MM	
Parameter number	:23	
Instance number	:6	
Makespan	:20	
Solution		
Job	Mode	Start time
1	1	0
2	1	0
3	2	0
4	2	4
5	1	8
6	2	4
7	1	12
8	1	20

Table 11

Format – Optimal solutions

Authors' name	:A.Author/C.Co-author
Authors' e-mail	:uve@test.uni-loaction.de
Authors' initials [ $\leq 3$ signs]	:AC
Shelfmark [ $\leq 3$ signs]	:95a
Instance set	:J30
Type	:SM
Date	:6/15/95

Research Report: New benchmark results for the resource-constrained project scheduling problem.

Computer	:IBM PC PS/2 Model P75
Processor	:80486
Clockpulse	:25 MHz
Operating system	:Windows NT
Memory code	:110 KB
Memory data	:16 MB
Language	:MS Visual C++
Average CPU-time	:33.68 sec.

Parameter	Instance	Makespan	CPU-time sec.
1	1	43	0.30
1	2	47	0.11
1	3	47	0.12
1	4	62	0.64
1	5	39	0.48

First, for the instance sets the optimal solutions of which are not known or verified so far, improved solutions can be sent via e-mail with the subject 'heuristicsolution'. The format has to be as specified in Table 10. Note, since we will check feasibility of the solutions automatically, it is necessary to meet the format exactly. The head of the file, line 1 through 4, has to be given once, the complete body, line 5 through 22, has to be repeated depending on the number of solutions suggested. A model file can be obtained by sending an e-mail with the subject 'heuristicformat' to the address given on the opening page. For each instance set, e.g., J30 of type MM, which has not been entirely solved to optimality so far, a file with the best makespans known, here J30HRS.MM, is accessible and will be updated each month at the end of its final week.

Second, for instance sets entirely solved to optimality, the optimal makespans and CPU-times for all problems of the set can be sent via e-mail with the subject 'optimalsolution'. Obviously, we cannot guarantee optimality of the makespans submitted.

Therefore, the solutions are only accepted if a research report or a publication in a journal describing the solution procedure can be referenced and is commonly accessible. Again, a model file can be obtained by sending an e-mail with the subject 'optimalformat' to the address provided in footnote 1. The format of an optimal makespan file is specified in Table 11. The results will be made available without change using the instance set specifier followed by the type specifier and the initials of the author(s). The shelfmark is used as extension. The example of Table 11 would produce file J30SMDH.95a.

Finally, e-mails sent to the authors which are of common interest are made available in the file LATENEWS.

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